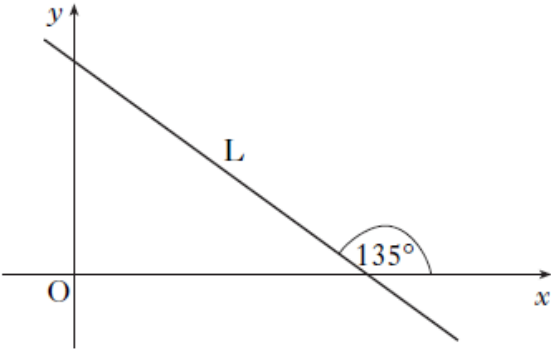


00 PI A3	3C $\bullet^1 \frac{2-(-1)}{3\sqrt{3}-0}$ $\bullet^2 \tan \alpha = \text{gradient}$ <i>stated or implied by</i> \bullet^3 $\bullet^3 \alpha = 30$
01 PI Q1	3C $\bullet^1 y = -\frac{2}{3}x + \frac{5}{3}$ stated $\bullet^2 m_{line} = -\frac{2}{3}$ stated $\bullet^3 y - (-1) = -\frac{2}{3}(x - 2)$ ans: $2x + 3y = 1$
3. (JAN) 02 P1	2C, 2C $\bullet^1 m = -1$ $\bullet^2 y - 5 = -1(x + 1)$ or $y - 1 = -1(x - 3)$ ans: $y + x = 4$ $\bullet^3 \tan(\text{angle}) = -1$ $\bullet^4 \text{angle} = 135^\circ$
4.(JAN) 02 P2	6C, 2C $\bullet^1 m_{PR} = 2$ stated $\bullet^2 \text{use } m_1 m_2 = -1 \Rightarrow m_{QS} = -\frac{1}{2}$ $\bullet^3 y - 4 = -\frac{1}{2}(x + 2)$ $\bullet^4 2y + x = 6$ or equivalent \bullet^5 strategy for sim. equ eg substitute $\bullet^6 T(2, 2)$ OR $\bullet^7 \text{strategy eg } \vec{TP} = \vec{RT}$ $\bullet^7 x_P = -1$ $\bullet^8 P(-1, -4)$ $\bullet^8 y_P = -4$
	3C, 4C, 1C $\bullet^1 F = \text{mid}_{AB} = (-2, 2)$ $\bullet^2 m_{FC} = 0$ stated or implied by \bullet^3 \bullet^3 equ FC is $y = 2$ $\bullet^4 M = \text{mid}_{BC} = (1, 0)$ $\bullet^5 m_{BC} = \frac{1}{2}$ $\bullet^6 m_{\perp} = -2$ ans : $y = 2$ $\bullet^7 y - 0 = -2(x - 1)$ ans : $y = -2x + 2$ $\bullet^8 (0, 2)$ ans : $(0, 2)$
03 P1	3C $\bullet^1 m = -4$ stated or implied by \bullet^2 $\bullet^2 m_{perp} = \frac{1}{4}$ $\bullet^3 y - 3 = \frac{1}{4}(x - (-1))$ ans: $x - 4y + 13 = 0$

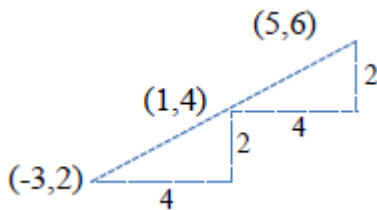
04 P1	<p>3C, 5C</p> <ul style="list-style-type: none"> •¹ $x = -3y - 1$ and attempt to substitute e.g. $2(-3y - 1) + \dots = 0$ •² $B(5, -2)$ •³ $m_{AB} = 3$ •⁴ $m_{AB} = 3 \Rightarrow m_{\text{perp}} = -\frac{1}{3}$ •⁵ $y = -\frac{1}{3}x \dots$ stated / implied by •⁶ •⁶ $m_{l_1} = -\frac{1}{3}$ •⁷ $m_{l_2} = -\frac{2}{5}$ •⁸ so only the 1st line is perpendicular to AB <p>OR</p> <ul style="list-style-type: none"> •⁴ $y = -\frac{1}{3}x \dots$ may be implied by •⁵ •⁵ $m_{l_1} = -\frac{1}{3}$ •⁶ $m_{l_2} = -\frac{2}{5}$ •⁷ $l_1 : 3 \times -\frac{1}{3} = -1$ so $AB \perp l_1$ •⁸ and AB is not $\perp l_2$ <p>OR</p> <ul style="list-style-type: none"> •⁴ $m_{AB} = 3 \Rightarrow m_{\text{perp}} = -\frac{1}{3}$ •⁵ $y = -\frac{2}{5}x$ stated / implied by •⁶ •⁶ $m_{l_1} = -\frac{2}{5}$ •⁷ $m_{l_2} = -\frac{1}{3}$ •⁸ so only the 2nd line is perpendicular to AB <p>OR</p> <ul style="list-style-type: none"> •⁴ $m_{\text{perp}} = -\frac{1}{3}$ •⁵ strat: find equ. thr' B with gradient $-\frac{1}{3}$ •⁶ $y - (-2) = -\frac{1}{3}(x - 5)$ •⁷ leading to $3y + x + 1 = 0$ •⁸ the first line is the ONLY line perp. to AB <p>OR</p> <ul style="list-style-type: none"> •⁴ $y = -\frac{1}{3}x \dots$ may be implied by •⁵ •⁵ $m_{l_1} = -\frac{1}{3}$ •⁶ $m_{l_2} = -\frac{2}{5}$ •⁷ $l_1 : 3 \times -\frac{1}{3} = -1$ so AB is the ONLY line $\perp l_1$ •⁸ implied by the "ONLY" at •⁷.
04 P2	<p>3C, 1C</p> <ul style="list-style-type: none"> •¹ gradient $= \frac{1}{2}$ •² $\tan a^\circ = \text{gradient}$ stated •³ $\tan^{-1}\left(\frac{1}{2}\right) = 26.6^\circ$

	<ul style="list-style-type: none"> •⁴ $m_{\angle} = \tan(30 + 26.6)^{\circ} = 1.5$ • $m_{OA} = \frac{1}{2}$ • $\tan a^{\circ} = \frac{1}{2}$ • $a = \tan^{-1}(\frac{1}{2}) = 26.6^{\circ}$ • $m_{OB} = \tan(30 + 26.6)^{\circ} = 1.5$
05 P1	3C <ul style="list-style-type: none"> •¹ $m = \tan(60^{\circ})$ stated •² $m = \sqrt{3}$ •³ $y - 0 = \sqrt{3}(x - (-2))$
06 P1	3C, 3C, 3C <ul style="list-style-type: none"> •¹ $D = (3, 5)$ •² $m_{BD} = 2$ •³ $y - 5 = 2(x - 3)$ or $y + 5 = 2(x - (-2))$ etc •⁴ $m_{BC} = \frac{1}{3}$ stated explicitly •⁵ $m_{alt} = -3$ •⁶ $y - 12 = -3(x - (-1))$ •⁷ $y - 5 = 2(x - 3)$ and $y - 12 = -3(x - (-1))$ or equivalent •⁸ $x = 2$ •⁹ $y = 3$
06 P2	4C, 2C <ul style="list-style-type: none"> •¹ $m_{PS} = 3$ •² $m_{QS} = -\frac{1}{3}$ •³ $y - 6 = -\frac{1}{3}(x - 4)$ To gain •⁴, some evidence of completion needs to be shown •⁴ completes proof e.g. $y - 6 = -\frac{1}{3}(x - 4)$ •⁵ $Q = (22, 0)$ $3(y - 6) = -(x - 4)$ •⁶ $R = (24, 6)$ $x + 3y = 22$
07 P1	3C <ul style="list-style-type: none"> •¹ $y = 3x....$ stated/IMPLIED by •² •² $gradient = 3$ stated/IMPLIED by •³ •³ $y - 4 = 3(x - (-1))$ or •¹ $form\ is\ 3x - y + c = 0$ •² $3 \times (-1) - 4 + c = 0$ •³ $c = 7$

08 P1	<p>7. The diagram shows a line L; the angle between L and the positive direction of the x-axis is 135°, as shown.</p>  <p>What is the gradient of line L?</p>
08 P2	<p>4C, 3C, 3C</p> <ul style="list-style-type: none"> •¹ $m_{BC} = -\frac{1}{2}$ <i>stated explicitly</i> •² $m_{\perp} = 2$ <i>stated / implied by •⁴</i> •⁸ midpoint of BC = (1, -3) •⁴ $y + 3 = 2(x - 1)$ and complete •⁵ midpoint of AB = (2, 4) •⁶ $m_{\text{median}} = -3$ •⁷ $y + 5 = -3(x - 5)$ or $y - 4 = -3(x - 2)$ •⁸ use $y = 2x - 5$ $y = -3x + 10$ •⁹ $x = 3$ •¹⁰ $y = 1$
09 P1	<p>1C, 3C, 4C</p> <ul style="list-style-type: none"> •¹ $P = (-3, 0)$ •² $m_{QR} = -2$ <i>or equivalent</i> •³ $m_{alt} = \frac{1}{2}$ <i>s / i by •⁴</i> •⁴ $alt : y - 0 = \frac{1}{2}(x + 3)$ •⁵ $QR : y + 2 = -2(x - 8)$ <i>or</i> $y - 6 = -2(x - 4)$ •⁶ e.g. $x - 2y = -3$ and $2x + y = 14$ <i>see Note 5 & Options</i> •⁷ $x = 5$ •⁸ $y = 4$

	<p>Option 1 for •⁵ to •⁸ :</p> <p>•⁵ $QR : y + 2 = -2(x - 8)$</p> <p>•⁶ $\frac{1}{2}(x + 3) = -2(x - 8) - 2$</p> <p>•⁷ $x = 5$</p> <p>•⁸ $y = 4$</p> <p>Option 2 for •⁵ to •⁸ :</p> <p>•⁵ $QR : y - 6 = -2(x - 4)$</p> <p>•⁶ $\frac{1}{2}(x + 3) = -2(x - 4) + 6$</p> <p>•⁷ $x = 5$</p> <p>•⁸ $y = 4$</p>		
10 P1	<table border="0"> <tr> <td style="vertical-align: top;"> <p>know and find midpoint of AC</p> <p>calculate gradient of BQ</p> <p>state equation</p> <p>substitute in for T</p> </td><td style="vertical-align: top;"> <p>•¹ (11, 10)</p> <p>•² $-\frac{6}{15}$ or equivalent</p> <p>•³ $y - 16 = -\frac{2}{5}(x - (-4))$ or $y - 10 = -\frac{2}{5}(x - 11)$</p> <p>•⁴ e.g. Substitution : $2(6) + 5(12) = 12 + 60 = 72$</p> <p>Gradients : $m_{BT} = -\frac{4}{10} = -\frac{2}{5} = m_{BQ}$</p> <p>Vectors : $\overrightarrow{BT} = \begin{pmatrix} 10 \\ -4 \end{pmatrix}$, $\overrightarrow{TQ} = \begin{pmatrix} 5 \\ -2 \end{pmatrix}$ and $\overrightarrow{BT} = 2\overrightarrow{TQ}$</p> <p>Method 1 : Vector approach</p> <p>valid method for finding the ratio •⁵ e.g. $\overrightarrow{BT} = \begin{pmatrix} 10 \\ -4 \end{pmatrix}$ and $\overrightarrow{TQ} = \begin{pmatrix} 5 \\ -2 \end{pmatrix}$</p> <p>complete to simplified ratio •⁶ 2 : 1</p> <p>Method 2 : "Stepping out" approach</p> <p>•⁵ e.g. $\begin{array}{ccc} & 10 & 5 \\ B & \text{---} & T & \text{---} & Q \\ & & & & \end{array}$ or $\begin{array}{ccc} B & T & Q \\ -4 & 6 & 11 \\ 10 & 5 & \end{array}$</p> <p>•⁶ 2 : 1</p> <p>Method 3 : Distance Formula approach</p> <p>•⁵ e.g. $d_{BT} = \sqrt{116}$ and $d_{TQ} = \sqrt{29}$</p> <p>•⁶ 2 : 1</p> </td></tr> </table>	<p>know and find midpoint of AC</p> <p>calculate gradient of BQ</p> <p>state equation</p> <p>substitute in for T</p>	<p>•¹ (11, 10)</p> <p>•² $-\frac{6}{15}$ or equivalent</p> <p>•³ $y - 16 = -\frac{2}{5}(x - (-4))$ or $y - 10 = -\frac{2}{5}(x - 11)$</p> <p>•⁴ e.g. Substitution : $2(6) + 5(12) = 12 + 60 = 72$</p> <p>Gradients : $m_{BT} = -\frac{4}{10} = -\frac{2}{5} = m_{BQ}$</p> <p>Vectors : $\overrightarrow{BT} = \begin{pmatrix} 10 \\ -4 \end{pmatrix}$, $\overrightarrow{TQ} = \begin{pmatrix} 5 \\ -2 \end{pmatrix}$ and $\overrightarrow{BT} = 2\overrightarrow{TQ}$</p> <p>Method 1 : Vector approach</p> <p>valid method for finding the ratio •⁵ e.g. $\overrightarrow{BT} = \begin{pmatrix} 10 \\ -4 \end{pmatrix}$ and $\overrightarrow{TQ} = \begin{pmatrix} 5 \\ -2 \end{pmatrix}$</p> <p>complete to simplified ratio •⁶ 2 : 1</p> <p>Method 2 : "Stepping out" approach</p> <p>•⁵ e.g. $\begin{array}{ccc} & 10 & 5 \\ B & \text{---} & T & \text{---} & Q \\ & & & & \end{array}$ or $\begin{array}{ccc} B & T & Q \\ -4 & 6 & 11 \\ 10 & 5 & \end{array}$</p> <p>•⁶ 2 : 1</p> <p>Method 3 : Distance Formula approach</p> <p>•⁵ e.g. $d_{BT} = \sqrt{116}$ and $d_{TQ} = \sqrt{29}$</p> <p>•⁶ 2 : 1</p>
<p>know and find midpoint of AC</p> <p>calculate gradient of BQ</p> <p>state equation</p> <p>substitute in for T</p>	<p>•¹ (11, 10)</p> <p>•² $-\frac{6}{15}$ or equivalent</p> <p>•³ $y - 16 = -\frac{2}{5}(x - (-4))$ or $y - 10 = -\frac{2}{5}(x - 11)$</p> <p>•⁴ e.g. Substitution : $2(6) + 5(12) = 12 + 60 = 72$</p> <p>Gradients : $m_{BT} = -\frac{4}{10} = -\frac{2}{5} = m_{BQ}$</p> <p>Vectors : $\overrightarrow{BT} = \begin{pmatrix} 10 \\ -4 \end{pmatrix}$, $\overrightarrow{TQ} = \begin{pmatrix} 5 \\ -2 \end{pmatrix}$ and $\overrightarrow{BT} = 2\overrightarrow{TQ}$</p> <p>Method 1 : Vector approach</p> <p>valid method for finding the ratio •⁵ e.g. $\overrightarrow{BT} = \begin{pmatrix} 10 \\ -4 \end{pmatrix}$ and $\overrightarrow{TQ} = \begin{pmatrix} 5 \\ -2 \end{pmatrix}$</p> <p>complete to simplified ratio •⁶ 2 : 1</p> <p>Method 2 : "Stepping out" approach</p> <p>•⁵ e.g. $\begin{array}{ccc} & 10 & 5 \\ B & \text{---} & T & \text{---} & Q \\ & & & & \end{array}$ or $\begin{array}{ccc} B & T & Q \\ -4 & 6 & 11 \\ 10 & 5 & \end{array}$</p> <p>•⁶ 2 : 1</p> <p>Method 3 : Distance Formula approach</p> <p>•⁵ e.g. $d_{BT} = \sqrt{116}$ and $d_{TQ} = \sqrt{29}$</p> <p>•⁶ 2 : 1</p>		
11 P1	<table border="0"> <tr> <td style="vertical-align: top;"> <p>find gradient of BD</p> <p>state equation of BD</p> </td><td style="vertical-align: top;"> <p>•¹ $\frac{15}{5}$ or equivalent</p> <p>•² $y - (-3) = 3(x - 2)$ or $y - 12 = 3(x - 7)$</p> </td></tr> </table>	<p>find gradient of BD</p> <p>state equation of BD</p>	<p>•¹ $\frac{15}{5}$ or equivalent</p> <p>•² $y - (-3) = 3(x - 2)$ or $y - 12 = 3(x - 7)$</p>
<p>find gradient of BD</p> <p>state equation of BD</p>	<p>•¹ $\frac{15}{5}$ or equivalent</p> <p>•² $y - (-3) = 3(x - 2)$ or $y - 12 = 3(x - 7)$</p>		

	<p>start solution of simultaneous equations</p> <p>solve for one variable</p> <p>solve for second variable</p> <p>know and find midpoint of AB</p> <p>find gradient of AB</p> <p>interpret perpendicular gradient</p> <p>state equation of perp. bisector</p> <p>justification of point on line</p>	<p>•³ e.g. $3x - y = 9$ and $x + 3y = 23$</p> <p>or $3x - 9 = -\frac{x}{3} + \frac{23}{3}$</p> <p>or $x + 3(3x - 9) = 23$</p> <p>•⁴ $x = 5$ or $y = 6$</p> <p>•⁵ $y = 6$ or $x = 5$</p> <p>•⁶ (3,10)</p> <p>•⁷ $\frac{4}{8}$ or equivalent</p> <p>•⁸ $-\frac{8}{4}$ or equivalent stated, or implied</p> <p>•⁹ $y - 10 = -2(x - 3)$ but not $y - 6 = -2(x - 5)$</p> <p>•¹⁰ when $x = 5$, $y = -2 \times 5 + 16 = 6$</p> <p>or</p> <p>$2 \times 5 + 6 - 16 = 0$</p>
12 P1	<p>find midpoint of PQ</p> <p>find gradient of PQ</p> <p>interpret perpendicular gradient</p> <p>state equation of perp. bisector</p> <p>use parallel gradients</p> <p>state equation of line</p> <p>use valid approach</p> <p>solve for one variable</p> <p>solve for other variable</p> <p>identify appropriate points</p> <p>calculate distance</p>	<p>•¹ (1, 3)</p> <p>•² -3</p> <p>•³ $\frac{1}{3}$</p> <p>•⁴ $y - 3 = \frac{1}{3}(x - 1)$</p> <p>•⁵ -3 stated, or implied</p> <p>•⁶ $y - (-2) = -3(x - 1)$</p> <p>•⁷ e.g. $x - 3y = -8$ and $9x + 3y = 3$</p> <p>or $-3x + 1 = \frac{1}{3}x + \frac{8}{3}$</p> <p>or $3(3y - 8) + y = 1$</p> <p>•⁸ e.g. $x = -\frac{1}{2}$</p> <p>•⁹ e.g. $y = \frac{5}{2}$</p> <p>•¹⁰ (1, 3) and $(-\frac{1}{2}, \frac{5}{2})$</p> <p>•¹¹ $\sqrt{\frac{5}{2}}$ accept $\frac{\sqrt{10}}{2}$ or $\sqrt{2 \cdot 5}$</p>
13 P2	<p>know to find gradient</p> <p>use perpendicular gradient</p> <p>state equation of line</p> <p>prepare to solve</p> <p>solve for one variable</p> <p>solve for second variable</p>	<p>•¹ $m_{PQ} = -2$</p> <p>•² $m_{QR} = \frac{1}{2}$</p> <p>•³ $y - 6 = \frac{1}{2}(x - 5)$</p> <p>•⁴ $x + 3y = 13$ and $x - 2y = -7$</p> <p>•⁵ $x = 1$ or $y = 4$</p> <p>•⁶ $y = 4$ or $x = 1$</p>

	<p>valid method eg vectors or stepping out or mid-point formula</p> <p>know how to find R</p> <p>know how to find S using $\overrightarrow{RS} = \overrightarrow{QP} = \begin{pmatrix} 2 \\ -4 \end{pmatrix}$</p> <p>Notes</p> <p>If R(-3,2) and S(-1,-2) appear without working then \bullet^7, \bullet^8 and \bullet^9 are not available.</p> <p>Eg </p>	<p>\bullet^7 eg $\overrightarrow{QT} = \begin{pmatrix} -4 \\ -2 \end{pmatrix}$</p> <p>$\bullet^8$ R(-3, 2)</p> <p>\bullet^9 S(-1, -2)</p> <p>OR</p> <table border="1" data-bbox="734 548 1165 772"> <tr> <td>\bullet^7</td><td>\bullet^8</td><td></td></tr> <tr> <td>$\frac{a+5}{2} = 1$</td><td>$\frac{b+6}{2} = 4$</td><td>\bullet^7</td></tr> <tr> <td>$a = -3$</td><td>$b = 2$</td><td>\bullet^8</td></tr> </table>	\bullet^7	\bullet^8		$\frac{a+5}{2} = 1$	$\frac{b+6}{2} = 4$	\bullet^7	$a = -3$	$b = 2$	\bullet^8
\bullet^7	\bullet^8										
$\frac{a+5}{2} = 1$	$\frac{b+6}{2} = 4$	\bullet^7									
$a = -3$	$b = 2$	\bullet^8									
14 P2	<p>find gradient of AB</p> <p>find perpendicular gradient</p> <p>find midpoint of AB</p> <p>obtain equation</p> <p>know to solve simultaneously</p> <p>solve correctly for x and y</p> <p>know and use $m = \tan \theta$</p> <p>calculate angle</p>	<p>\bullet^1 $m_{AB} = 1$</p> <p>\bullet^2 $m_{\text{perp}} = -1$ stated or implied by \bullet^4</p> <p>\bullet^3 (4,1) stated or implied by \bullet^4</p> <p>\bullet^4 $y - 1 = -1(x - 4)$</p> <p>\bullet^5 $y + 2x = 6$ $y + x = 5$</p> <p>\bullet^6 $x = 1, y = 4$</p> <p>\bullet^7 $\tan \theta = -2$</p> <p>\bullet^8 116.6°</p> <p>accept 117^0 or 2.03 radians</p>									
	<p>know and find midpoint of AC</p> <p>calculate gradient of BQ</p> <p>state equation</p> <p>substitute in for T</p>	<p>\bullet^1 (11, 10)</p> <p>\bullet^2 $-\frac{6}{15}$ or equivalent</p> <p>\bullet^3 $y - 16 = -\frac{2}{5}(x - (-4))$ or $y - 10 = -\frac{2}{5}(x - 11)$</p> <p>$\bullet^4$ e.g. Substitution : $2(6) + 5(12) = 12 + 60 = 72$</p> <p>Gradients : $m_{BT} = -\frac{4}{10} = -\frac{2}{5} = m_{BQ}$</p> <p>Vectors : $\overrightarrow{BT} = \begin{pmatrix} 10 \\ -4 \end{pmatrix}, \overrightarrow{TQ} = \begin{pmatrix} 5 \\ -2 \end{pmatrix}$ and $\overrightarrow{BT} = 2\overrightarrow{TQ}$</p>									

	<p>Method 1 : Vector approach</p> <p>valid method for finding the ratio •⁵ e.g. $\overrightarrow{BT} = \begin{pmatrix} 10 \\ -4 \end{pmatrix}$ and $\overrightarrow{TQ} = \begin{pmatrix} 5 \\ -2 \end{pmatrix}$</p> <p>complete to simplified ratio •⁶ 2 : 1</p> <p>Method 2 : “Stepping out” approach</p> <p>•⁵ e.g. $\begin{array}{c} \text{B} \quad \text{T} \quad \text{Q} \\ \text{---} 10 \text{---} 5 \text{---} \\ \text{B} \quad \text{T} \quad \text{Q} \end{array}$ or $\begin{array}{c} \text{B} \quad \text{T} \quad \text{Q} \\ -4 \quad 6 \quad 11 \\ 10 \quad 5 \end{array}$</p> <p>•⁶ 2 : 1</p> <p>Method 3 : Distance Formula approach</p> <p>•⁵ e.g. $d_{BT} = \sqrt{116}$ and $d_{TQ} = \sqrt{29}$</p> <p>•⁶ 2 : 1</p>
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ANSWERS - PRE 2000 - Concurrency

1	<ul style="list-style-type: none"> •¹ know to solve 2 equ & check in 3rd •² 1 coord. of $(5, -2)$ or $(\frac{14}{3}, -\frac{16}{9})$ or $(\frac{41}{8}, -\frac{13}{8})$ •³ second appropriate coordinate •⁴ checking $(5, -2)$ does not lie on 3rd line or $(\frac{14}{3}, -\frac{16}{9})$ not on 2nd line or $(\frac{41}{8}, -\frac{13}{8})$ not on 1st line
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ANSWERS - PRE 2000 - Gradient (m = tan Θ)

1	<ul style="list-style-type: none"> •¹ $m_{AB} = \frac{4b^2 - a^2}{2b - a}$ •² $m_{AB} = \frac{(2b + a)(2b - a)}{2b - a} = 2b + a$
2	<ul style="list-style-type: none"> •¹ $\tan a^\circ = 2$ •² $a = 63.4^\circ$ •³ $\tan(180 - b) = 1$ •⁴ $b = 135$ •⁵ $180 - a - (180 - b)$ or equiv. to $b - a$
3	<ul style="list-style-type: none"> •¹ “correct angle” = $\frac{\pi}{2} - \frac{\pi}{3}$ •² $\frac{1}{\sqrt{3}}$
4	<ul style="list-style-type: none"> •¹ strat: i.e. try to evaluate \hat{COA} •² $\hat{AOB} = 36.9^\circ$ •³ $\tan 73.7^\circ = 3.428$
5	<ul style="list-style-type: none"> ▪ $OB = 5$ •³ $\hat{BOX} = 36.9^\circ$ •⁴ $\hat{ROB} = 67.4^\circ$ •¹ know to find $\tan \hat{ROX} = 104^\circ$ •⁵ $m_{RO} = -3.9$

ANSWERS - PRE 2000 Collinearity

1	<ul style="list-style-type: none"> •¹ strat: <i>compare</i> gradients •² $m_{A_1A_2} = \frac{2}{3}$ •³ $m_{A_2S} = \frac{1}{2}$ or $m_{A_1S} = \frac{5}{9}$ so not heading for S •⁴ $m_{B_1B_2} = \frac{5}{4}$ •⁵ $m_{B_2S} = \frac{5}{4}$ or $m_{B_1S} = \frac{5}{4}$ so heading for S 	<ul style="list-style-type: none"> •¹ strat: st lines and substitution •² $A_1A_2: y+1 = \frac{2}{3}(x+4)$ or equivalent •³ $4+1 \neq \frac{2}{3}(5+4)$ so not heading for S •⁴ $B_1B_2: y+11 = \frac{5}{4}(x+7)$ or equivalent •⁵ $4+11 = \frac{5}{4}(5+7)$ so heading for S
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ANSWERS - PRE 2000 Parallel and Perpendicular Lines

1	<ul style="list-style-type: none"> •¹ $m = -\frac{3}{2}$ stated or implied by •² •² $y - (-5) = -\frac{3}{2}(x - 3)$ <p style="text-align: right;">ans: $3x + 2y + 1 = 0$</p>
2	<ul style="list-style-type: none"> •¹ $m_{OA} = -\frac{3}{2}$ •² $m_{\perp} = \frac{2}{3}$ •³ $y - 3 = \frac{2}{3}(x + 2)$ <p style="text-align: right;">eqn: $2x - 3y + 13 = 0$</p> <ul style="list-style-type: none"> • $2(-5) - 3(1) + 13 = -10 - 3 + 13 = 0$, so $(-5, 1)$ lies on this line and Brenda is standing on Newport Road.
3	<p>(a)</p> <ul style="list-style-type: none"> •¹ $m_{PR} = 2$ •² PR: e.g. $y + 2 = 2(x - 1)$ •³ knowing to use $m_1m_2 = 1$ for m_{QS} •⁴ $m_{QS} = -\frac{1}{2}$ •⁵ QS: e.g. $y - 3 = -\frac{1}{2}(x - 6)$ •⁶ knowing to solve simultaneously •⁷ $S = (4, 4)$ <p>(b)</p> <ul style="list-style-type: none"> •⁸ $\vec{QM} = \vec{MS}$ or equivalent indication •⁹ $S = (2, 5)$
4	<p>(a)</p> <ul style="list-style-type: none"> •¹ using $m_1m_2 = -1$ •² $m_{AD} = -2$ •³ $y - 4 = -2(x - 3)$ <p>(b)</p> <ul style="list-style-type: none"> •⁴ strategy for sim. equations •⁵ $2x + y = 10$ or equiv •⁶ $(4, 2)$ <p>(c)</p> <ul style="list-style-type: none"> •⁷ strategy : find length of AD •⁸ 5

ANSWERS - PRE 2000 **Perpendicular Bisectors**

1	<ul style="list-style-type: none"> •¹ $m_{AB} = \frac{3}{4}$ •² $y - 5 = \frac{3}{4}(x - 5)$ or $y - (-1) = \frac{3}{4}(x - (-3))$ ans : $3x - 4y + 5 = 0$ •³ $m_{\perp} = -\frac{4}{3}$ •⁴ midpoint = (1, 2) •⁵ $y - 2 = -\frac{4}{3}(x - 1)$ ans: $4x + 3y - 10 = 0$
2	<ul style="list-style-type: none"> •¹ midpt = (1, 1) •² $m_{AB} = -\frac{2}{3}$ •³ $m_{diam} = \frac{3}{2}$ •⁴ $y - 1 = \frac{3}{2}(x - 1)$
3	<ul style="list-style-type: none"> •¹ midpoint = (5, 1) •² $m_{AB} = \frac{2}{3}$ •³ $m_{\perp} = -\frac{3}{2}$ •⁴ $y - 1 = -\frac{3}{2}(x - 5)$ ans: $3x + 2y - 17 = 0$
4	<p>(a)</p> <ul style="list-style-type: none"> •¹ $m_{BC} = -\frac{1}{3}$ •² $m_{\perp} = 3$ •³ midpoint_{BC} = $(\frac{9}{2}, \frac{5}{2})$ •⁴ $y - \frac{5}{2} = 3(x - \frac{9}{2})$ ans: $3x - y - 11 = 0$ •⁶ perp. bisector passes thr' centre stated explicitly <p>(b)</p> <ul style="list-style-type: none"> •⁷ using $y - 3x = -11$ and $y + 2x = 4$ or equivalent equations •⁸ (3, -2)
5	<p>2C, 2C</p> <ul style="list-style-type: none"> • $m_{AB} = -1$ • $x + y - 4 = 0$ $y - 5 = -1(x + 1)$ or $y - 1 = -1(x - 3)$ • $\tan(\text{angle}) = -1$ • $\text{angle} = 135^\circ$ • $AB = \sqrt{((7 - -1)2 + (-3 - 5)2)} = \sqrt{(128)}$ • $AB = 8\sqrt{2} (= 11.3)$ • $m_{\text{perp}} = 1$ (& A(-1, 5)) • $x - y + 6 = 0$ • $M_{AB} (3, 1)$ (& $m = 1$) • $x - y - 2 = 0$

ANSWERS - PRE 2000 **Lines in Triangles**

1	<p>ans: $4x + 3y - 1 = 0$</p> <ul style="list-style-type: none"> •¹ $D = (1, -1)$ •² use A and D to get $m_{AD} = -\frac{4}{3}$ •³ $y - 3 = -\frac{4}{3}(x - -2)$
2	<p>ans: $2x - y - 5 = 0$</p> <ul style="list-style-type: none"> •¹ $M = (2, -1)$ •² $m_{AM} = 2$ •³ $y - (-1) = 2(x - 2)$
3	<p>ans: $2x + y + 3 = 0$</p> <ul style="list-style-type: none"> •¹ $m_{QR} = \frac{1}{2}$ •² $m_{PN} = -2$ • PS : $y - 5 = -2(x - (-4))$
4	<p>ans: $8x - y + 7 = 0$</p> <ul style="list-style-type: none"> •¹ $m_{QR} = -\frac{1}{8}$ •² $m_{\perp} = 8$ •³ $y - (-1) = 8(x - (-1))$
5	<p>ans: CE $3x + y - 5 = 0$ BD $x - y + 1 = 0$ J (1, 2)</p> <ul style="list-style-type: none"> •¹ $E = (2, -1)$ •² $m_{CE} = -3$ •³ $y - (-1) = -3(x - 2)$ or $y - 8 = -3(x - (-1))$ •⁴ $m_{AC} = -1$ •⁵ $m_{BD} = -1$ •⁶ $y - (-2) = 1(x - (-3))$ •⁷ strat: attempt to solve simultaneously •⁸ J = (1, 2)
6	<p>(a) •¹ Calculate the length of the sides •² $AB = AC = \sqrt{3^2 + 6^2}$</p> <p>(b) •³ knows to find equ. of an altitude •⁴ $m_{AC} = -2$ •⁵ $m_{BE} = \frac{1}{2}$ •⁶ $y - 2 = \frac{1}{2}(x - 1)$ •⁷ $x = 4$ stated or implied •⁸ knows how to find intersection •⁹ $H = (4, \frac{7}{2})$ •¹⁰ $DA = 6$ and $DH = 1\frac{1}{2}$</p>

7	<p>(a)</p> <ul style="list-style-type: none"> •¹ midpoint = $(4, 2)$ •² $m_{MC} = -3$ •³ $y - 2 = -3(x - 4)$ or $y - (-7) = -3(x - 7)$ <p>(b)</p> <ul style="list-style-type: none"> •⁴ $m_{BC} = 2$ •⁵ $m_{\perp} = -\frac{1}{2}$ •⁶ $y - 1 = -\frac{1}{2}(x - (-4))$ <p>(c)</p> <ul style="list-style-type: none"> •⁷ e.g. $3x + y = 14$ and $x + 2y = -2$ •⁸ attempt to eliminate a variable •⁹ $(6, -4)$
8	<p>(a)</p> <ul style="list-style-type: none"> •¹ $m_{AB} = 2$ •² $m_{BC} = -\frac{1}{2}$ •³ $m_{AB} \times m_{BC} = -1 \Rightarrow m_{AB} \perp m_{BC}$ <p>(b)</p> <ul style="list-style-type: none"> •⁴ $D = (3, -1)$ and $E = (2, -3)$ •⁵ $m_{AD} = \frac{1}{3}$ •⁶ AD: $y + 1 = \frac{1}{3}(x - 3)$ or equiv. •⁷ $m_{BE} = -\frac{4}{3}$ •⁸ BE: $y - 1 = -\frac{4}{3}(x + 1)$ or equiv. •⁹ eg clear fractions •¹⁰ eg substitute •¹¹ $x = 1, y = -\frac{5}{3}$